

Rational Overoptimism and Limited Liability

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EXUBERANCE IN CREDIT BOOM-AND-BUSTS

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 2. ...but they are characterized with **lower risk premia** (Krishnamurthy & Muir, 2017)
 3. ...and they *predict* **negative excess return** on bank stock (Baron and Xiong, 2017)
- ⇒ **Systematic excess risk taking** during credit booms

EXISTING THEORIES

- Two alternative narratives in the literature:

1. **Limited liability** (Martinez-Miera & Repullo, 2017; Coimbra & Rey, 2020)

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- Two alternative narratives in the literature:

1. **Limited liability** (Martinez-Miera & Repullo, 2017; Coimbra & Rey, 2020)

- ▶ Motivated by risk taking incentives in payoff structure

2. **Behavioral overoptimism** (Bordalo et al, 2020; Krishnamurthy & Li, 2021)

- ▶ Motivated by evidence of systematic overoptimistic beliefs in booms

⇒ I show how overoptimism can be a result of limited liability

THIS PAPER/1

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1. **Rational overoptimism** from *information frictions*
 1. Aggregate factors increase default risk in booms
 2. Agents don't perfectly observe aggregate risk factors
- ⇒ Rational overoptimism about revenues during credit booms

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- Theory of procyclical **rational overoptimism** driven by **limited liability**
1. **Rational overoptimism** from *information frictions*
 1. Aggregate factors increase default risk in booms
 2. Agents don't perfectly observe aggregate risk factors⇒ Rational overoptimism about revenues during credit booms
 2. *Information frictions* can result from **limited liability**
 1. Agents can acquire information on risk factors
 2. Limited liability on payoff structure (e.g. managers compensation)⇒ Limited liability disincentives attention to risk factors

THIS PAPER/2

3. Model reproduces **key empirical features** of credit booms

1. Financial crises more likely after credit booms (Schularick and Taylor, 2012)
2. Financial crises more likely after decline in risk premia (Krishnamurthy and Muir, 2017)
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POLICY IMPLICATIONS

- Overoptimism results from risk-taking incentives in payoff structure
- ⇒ **Reducing limited liability** (e.g. regulating compensation)
- ▶ Encourage managers and shareholders to acquire information on risk
 - ▶ Reduces overoptimism in booms and mitigates boom&bust

CONTRIBUTION TO THE LITERATURE

1. Behavioral models of overoptimism

Gennaioli and Shleifer (2018), Bordalo et al (2018, 2020), Gabriel Chodorow-Reich et al (2021)

- ▶ Overoptimism from *behavioral overreaction* to good news
- ▶ **This paper:** Overoptimism from *rational underreaction* to bad news

2. Dispersed information with strategic interactions

Morris and Shin (2002), Angeletos and Lian (2017), Kohlhas and Walther (2020)

- ▶ Strategic substitutability + dispersed information \Rightarrow amplification
- ▶ **This paper:** Inattention from limited liability

3. Compensation incentives and information

Mackowiak and Wiederholt (2012), Lindbeck and Weibull (2017), Cole et al (2014)

- ▶ Limited liabilities lead to lower attention
- ▶ **This paper:** Embed in macro-finance model & empirical micro-evidence

Model environment

MODEL ENVIRONMENT

Model equations

- Continuum of “islands” inhabited by one firm and one bank
- *Local firm*
 - ▶ Start with zero capital, borrow to finance production
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- *Aggregate final good producer*
 - ▶ Buy intermediate goods from all firms
 - ▶ **Strategic substitutability**: \uparrow aggregate production, \downarrow interm price & \downarrow revenues

TIIMELINE

- Three stages

1. Information choice

Stage 1 eq

2. Observe information, decide borrowing and investment

Stage 2 eq

3. Shocks realization and payoff

PE AND GE EFFECTS

- Aggregate booms associated with a *positive* and *negative* effect

$$\underbrace{\ln A_j}_{\text{local TFP}} = \underbrace{e_j}_{\text{local shock}} + \underbrace{\theta}_{\text{aggregate TFP}}$$

- After an aggregate shock θ
 - ▶ \uparrow Local TFP $\ln A_j$: **positive PE effect**
 - Stronger fundamentals: \uparrow expected revenues, \uparrow investment
 - ▶ \uparrow Aggregate TFP θ : **negative GE effect**
 - Endogenous \uparrow in aggregate supply, \downarrow price \Rightarrow \downarrow expected revenues, \downarrow investment

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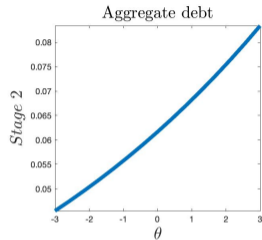
- After an aggregate shock θ
 - ▶ \uparrow Local TFP $\ln A_j$: **positive PE effect**
 - Stronger fundamentals: \uparrow expected revenues, \uparrow investment
 - ▶ \uparrow Aggregate TFP θ : **negative GE effect**
 - Endogenous \uparrow in aggregate supply, \downarrow price \Rightarrow \downarrow expected revenues, \downarrow investment
- Aggregate TFP θ (i.e. competitors decisions) harder to observe
- First limit cases: θ observed (*FI*) and not (*DI*), then I endogenize info choice

Full information model

FULL INFORMATION

- Suppose all islands decide to observe θ

1. Investment and debt \uparrow in agg shock

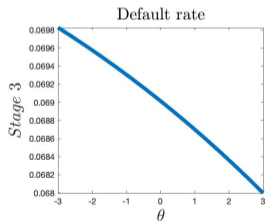
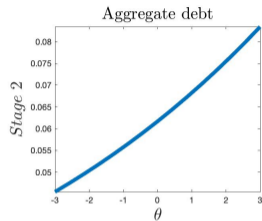


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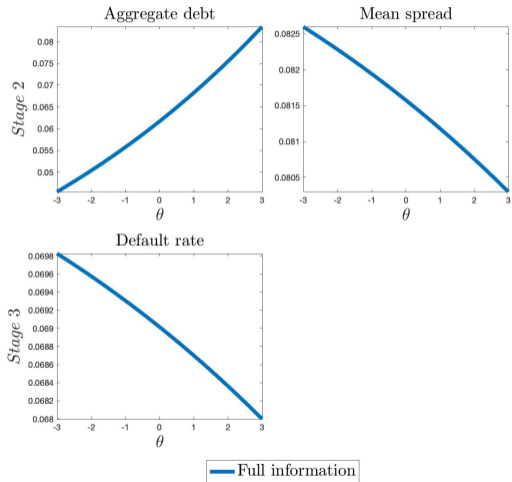
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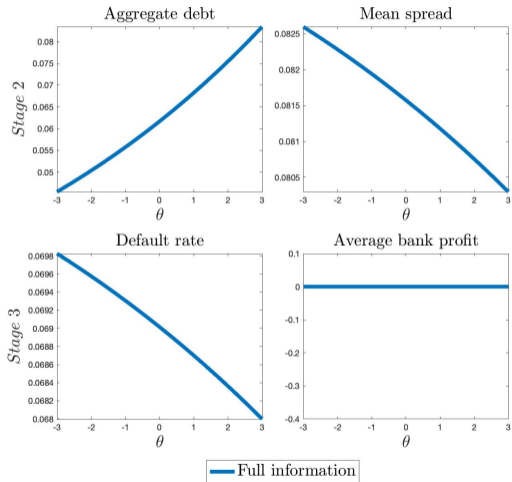
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 4. Bank's excess returns equal always zero
(Baron and Xiong, 2017)
- Economy not riskier after a credit boom \rightarrow **not match the evidence!**



Dispersed information model

DISPERSED INFORMATION

- Suppose now agents don't observe aggregates

Evidence on info friction

$$\underbrace{\ln A_j}_{\text{local TFP}} = \underbrace{e_j}_{\text{local shock}} + \underbrace{\theta}_{\text{aggregate TFP}}$$

- They can't tell if $\ln A_j \uparrow$ due to local shock $e_j \uparrow$ or aggregate shock $\theta \uparrow$

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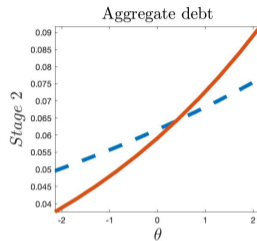
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- When $\theta \uparrow$, they partially confound it for $e_j \rightarrow$ **rationally confused**
- Underestimate \uparrow in agg supply & \downarrow in prices \rightarrow **overoptimistic** about own profit
- Over-borrow and over-invest, $\uparrow\uparrow$ supply and $\downarrow\downarrow$ prices even more \rightarrow **boom&bust**

Rationally extrapolative beliefs

DISPERSED INFORMATION

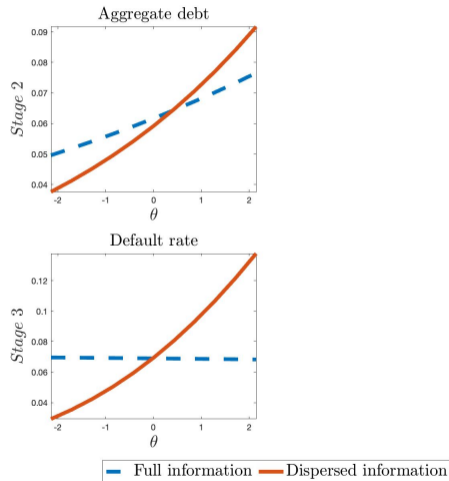
- Suppose no island observes θ
 1. Credit boom *amplified* by info friction



— Full information — Dispersed information

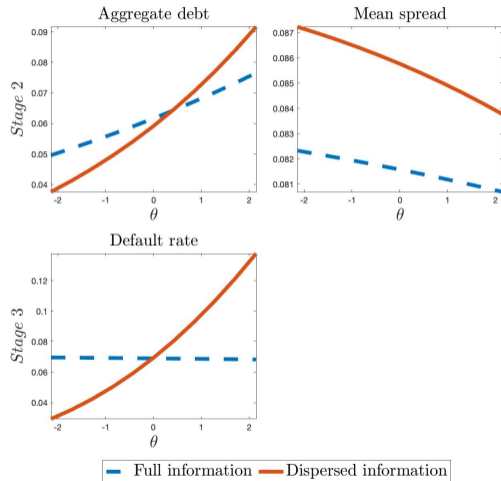
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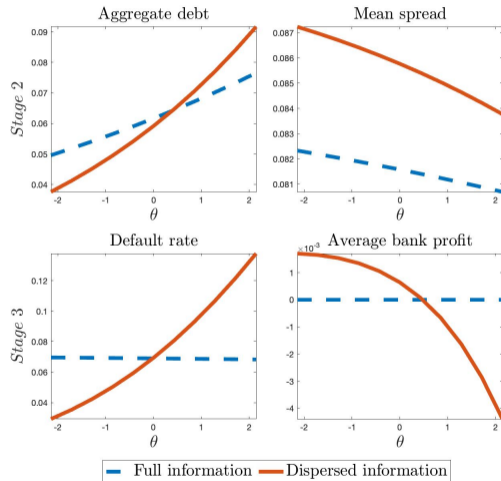
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DISPERSED INFORMATION

- Suppose no island observes θ
 1. Credit boom *amplified* by info friction
 2. Default risk *increases* after booms (Schularick and Taylor, 2012)
 3. Lower spreads predict *higher* default rate (Krishnamurthy and Muir, 2017)
 4. Bank's returns *negative* after a boom (Baron and Xiong, 2017)
- Economy riskier after a credit boom
→ **match the evidence!**



Endogenous information choice

INATTENTION DUE TO LIMITED LIABILITY

1. Allow agents to observe aggregates by paying an attention cost

(Mackowiak et al, 2020)

- ▶ Set info cost low such that still optimal to collect information

Info choice problem

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Info choice problem

- ▶ Set info cost low such that still optimal to collect information

2. Introduce limited liability on firm and bank payoff structure

Payoffs

- ▶ Higher LL ψ , higher insurance from company's losses

- ▶ Interpretation: public bailout, gvnmt guarantees on loan, managers option compensation, ...

⇒ **Higher limited liability** leads to **lower attention** choice

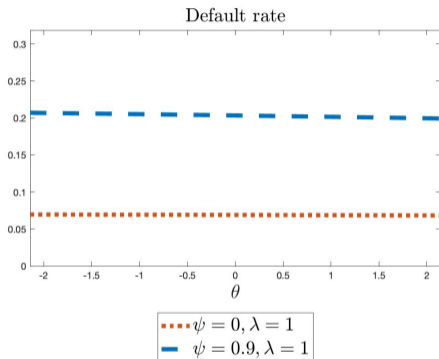
Graph

LIMITED LIABILITY INCENTIVES IN STAGES 1 & 2

- Limited liability $\psi > 0$ has two effects:
 - ▶ **Stage 1: Risk-taking in information:** lower information choice
 - ▶ **Stage 2: Risk-taking in investment:** for a given information
- I show that standard risk taking channel is not enough to match the evidence

RISK TAKING CHANNELS

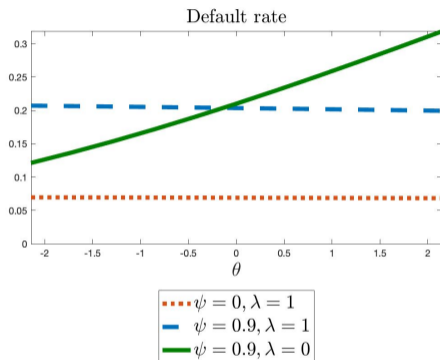
- **Dotted red:**
 $\psi = 0 \rightarrow$ endogenously full info
- **Dashed blue:**
 $\psi > 0$ but *assume* full info
(Risk taking in **investment**)



RISK TAKING CHANNELS

- **Dotted red:**
 $\psi = 0 \rightarrow$ endogenously full info
- **Dashed blue:**
 $\psi > 0$ but *assume* full info
(Risk taking in **investment**)
- **Solid green:**
 $\psi > 0 \rightarrow$ endogenously dispersed info
(Risk taking in **information** and **investment**)

\Rightarrow Limited liability effect on *information* explains evidence



ADDITIONAL RESULTS

1. **Analytical results:** characterization of full & dispersed information equilibrium
2. **Quantitative results:** paths of spread and credit in model consistent with the data

POLICY IMPLICATIONS

- Model implies **unexpected boom-and-busts**
 - ▶ Agents take excessive risk because they are uninformed
 - ▶ If agents were fully informed, they would reduce risk-taking
 - **Policy implication:** correct risk taking incentives
 - ▶ Lower limited liability encourages agents to pay attention to risk factors
 - ▶ E.g. regulating managers compensation
- ⇒ Correcting ***incentives*** reduces ***overoptimism*** and mitigates boom&bust

CONCLUSION

- I develop a theory of overoptimism-driven credit boom&bust, where
 - ▶ **Overoptimism** results *rationally* from inattention to risk
 - ▶ Inattention to risk may be driven by **risk taking** incentives in information choice
- The model is able to match the existing **macro-evidence** on **credit boom&busts**
- **Attenuating limited liability** can encourage agents to correctly assess risk

Thank you!

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Appendix

EVIDENCE ON CONTEMPORANEOUS BELIEF UNDER-REACTION

- *Contemporaneous* forecast errors: $fe_t = x_t - f_t(x_t)$
 - ▶ x_t → average macroeconomic quantity from quarter t to $t + 3$ (very short horizon)
 - ▶ $f_t(x_t)$ → forecast on x_t released in quarter t (*Survey of Professional Forecasters*)

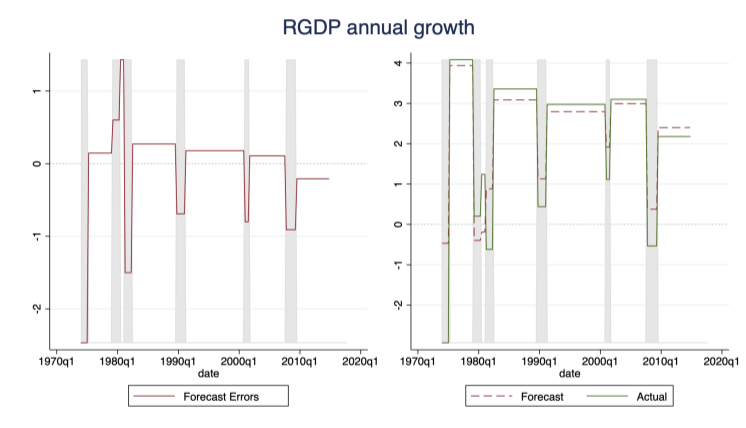
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- $fe_t > 0$ in *booms* (& $fe_t < 0$ in *busts*) ⇒ beliefs **under-react** to news
 - ▶ When $x \uparrow$, fx don't \uparrow enough (& when $x \downarrow$, fx don't \downarrow enough)
 - ▶ Consistent with **information frictions**

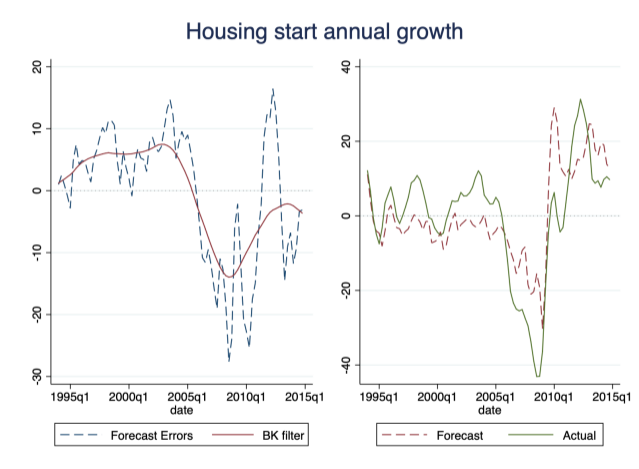
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- $fe_t < 0$ in *booms* (& $fe_t > 0$ in *busts*) ⇒ beliefs **over-react** to news
 - ▶ When $x \uparrow$, $fx \uparrow$ too much (& when $x \downarrow$, $fx \downarrow$ too much)
 - ▶ Consistent with **behavioral extrapolation**

BELIEF UNDER-REACTION: BUSINESS CYCLE



BELIEF UNDER-REACTION: HOUSING BOOM



EVIDENCE FOR INFORMATION FRICTIONS

- Belief data consistent with models of **information frictions**
- Additional existing evidence on information friction
 - ▶ Large information dispersion measured in forecast surveys
(*Coibion and Gorodnichenko, 2015; Gemmi and Valchev, 2021*)
 - ▶ Managers' expectations display more disagreement than professional forecasters
(*Coibion et al, 2018*)
- I propose a model where **overoptimism** results from *information frictions*

FIRM

- **Stage 2** borrow b_j at rate $r_j(b_j)$ to finance purchase of cap k_j

$$b_j = k_j + \phi \frac{k_j^2}{2}$$

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- **Stage 3** produce interm good $M_j = A_j^\zeta k_j^{\tilde{\alpha}} l_j^{1-\tilde{\alpha}}$, with profits $\pi_j = p_j M_j - \bar{w} l_j$

$$d_{firm,j} = \begin{cases} (1 - \tau)(\pi_j - (1 + r_j)b_j) & \text{if } \pi_j \geq (1 + r_j)b_j \quad (\text{repay}) \\ -c_d k_j, & \text{if } \pi_j < (1 + r_j)b_j \quad (\text{default}) \end{cases}$$

where c_d is a default cost

BANK

- Deep-pockets
- **Stage 2:** Borrow at (exogenous) risk free rate r^f to lend to the firm at risky rate r_j
- **Stage 3:** Bank's excess return

$$d_{bank,j} = \begin{cases} (r_j - r^f)b_j & \text{if } \pi_j \geq (1 + r_j)b_j \quad (\text{repay}) \\ -b_j(1 + r^f) & \text{if } \pi_j < (1 + r_j)b_j \quad (\text{default}) \end{cases}$$

FINAL GOOD PRODUCER

- **Stage 3:** purchase input $M = \left[\int^j M_j^\xi dj \right]^{\frac{1}{\xi}}$ and produce $Y = M^\nu$
- Demand function for good j

$$p_j = \nu M^{\nu-\xi} M_j^{\xi-1}$$

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- I assume $\nu < \xi \Rightarrow$ **strategic substitutability** between islands
 - ▶ If $\uparrow M$, then $\downarrow p_j$ and $\downarrow M_j$
 - ▶ It holds with standard calibration and consistent with IO estimates

Conditions for $\nu < \xi$

TECHNOLOGY SHOCKS

- **Stage 3:** island's technology realizes

$$\underbrace{\ln A_j}_{\text{local TFP}} = \underbrace{\epsilon_j}_{\text{local shock}} + \underbrace{\theta}_{\text{aggregate shock}}$$

- ▶ Local shock $\epsilon_j \sim N(0, \sigma_\epsilon^2)$, $\int^j \epsilon_j dj = 0$
- ▶ Aggregate shock $\theta \sim N(0, \sigma_\theta^2)$

⇒ Heterogeneous investment decisions

Back

STRATEGIC SUBSTITUTABILITY THROUGH PRICES

- Suppose final good sector
 - ▶ production function $Y = M^{\tilde{\nu}} X^{1-\tilde{\nu}}$ with $\tilde{\nu} = 0.5$
 - ▶ face a demand function $P = Y^{\frac{1}{\mu^F}-1}$ where $\mu^F > 1$ is the markup
 - ▶ Maximizing X out, profit function equal $\pi \propto M^{\frac{\tilde{\nu}}{\mu^F-(1-\tilde{\nu})}} \equiv M^\nu$
- Therefore $\nu < \xi$ implies

$$\mu^F > \frac{1 + \mu^I}{2}, \quad \mu^I \equiv 1/\xi > 1$$

- Satisfied as long as μ^F is **not** much lower μ^I
- In data, retail sector has the largest markup (*De Loecker et al, 2020*)

STAGE 1: INFORMATION CHOICE

- Pay cost c_{info} to observed θ perfectly in next stage
 - ▶ Firm and bank managers decide through Nash bargaining
- Pay cost if

$$E[d_{firm,j}^*(\theta \in \Omega_j, \lambda) - c_{info}] > E[d_{firm,j}^*(\theta \notin \Omega_j, \lambda)]$$

- ▶ Ω_j island j 's information set: $\theta \in \Omega_j$ or $\theta \notin \Omega_j$

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- ▶ Ω_j island j 's information set: $\theta \in \Omega_j$ or $\theta \notin \Omega_j$
- ▶ $\lambda \in [0, 1]$ Share of islands that pay the cost and are informed
 - $\lambda = 1$: Full information case
 - $\lambda = 0$: Dispersed information case
- Equilibrium λ^* st everybody is indifferent:
 $E[d_{firm,j}^*(\theta \in \Omega_j, \lambda^*) - c] = E[d_{firm,j}^*(\theta \notin \Omega_j, \lambda^*)]$

STAGE 2 - INFORMATION STRUCTURE

- Firm and bank in island j share all information
- They receive up to two signals

(1) *Free* signal on **local technology**

$$z_j = \ln(A_j) + \eta_j, \quad \eta_j \sim N(0, \sigma_\eta^2)$$

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(2) *Costly* signal on **aggregate technology** θ (or quantity M)

- ▶ Lucas island setting \rightarrow aggregates not freely observable
- ▶ They are able to observe aggregates if they paid information cost in stage 1

STAGE 2 - LENDING AND BORROWING

- Firm and bank decide debt b_j and loan rate r_j
 - ▶ I assume Nash bargaining with all bargaining power on firms
 - ▶ **Loan rate:** $E[d_{bank}|\Omega_j] = 0 \rightarrow \text{spread} \propto \text{perceived default prob}$

$$\frac{1 + r_j}{1 + r^f} = \frac{1}{1 - p(\text{default}(A_j, b_j, r_j, M)|\Omega_j)}$$

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- ▶ **Loan quantity:** The firm internalizes $r_j(b_j)$ and maximize expected profit

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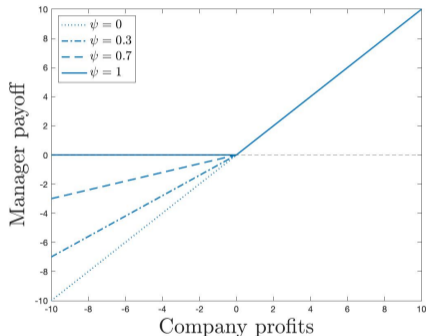
$$b_j = \text{argmax} E[d_{firm}(A_j, b_j, r_j(b_j), M)|\Omega_j]$$

- **Strategic substitutability:** $\uparrow M(\theta), \downarrow p_j \Rightarrow \downarrow b_j$ and M_j

MANAGER'S COMPENSATION

- Firms and banks run by managers
- Managers own $(1 - \psi)$ shares and ψ options
 - ▶ Assume zero exercise price and option in the money when $\pi > 0$

$$w = \begin{cases} \pi & \text{if } \pi \geq 0 \quad (\text{repay}) \\ (1 - \psi)\pi & \text{if } \pi < 0 \quad (\text{default}) \end{cases}$$



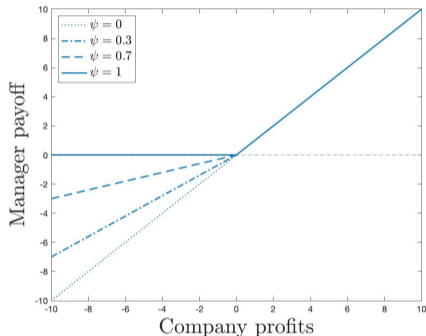
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- I map CEO's compensation to the data
- In general, ψ as any source of limited liability (public bailout or guarantees, etc)



MANAGER'S COMPENSATION

- Firm manager's payoff is given by

$$w_{firm,j} = \begin{cases} (1 - \tau)[\pi(A_j, k_j, M) - (1 + r_j)b_j] & \text{if } \pi(A_j, k_j, M) \geq (1 + r_j)b_j \\ -(1 - \psi)c_d k_j, & \text{if } \pi(A_j, k_j, M) < (1 + r_j)b_j \end{cases}$$

- ▶ Alternatively, lower c_d as moral hazard between borrower and lender

- Bank manager's payoff is given by

$$w_{bank,j} = \begin{cases} [(1 + r_j) - (1 + r^f)]b_j & \text{if } \pi(A_j, k_j, M) \geq (1 + r_j)b_j \\ -(1 - \psi)(1 + r_j)b_j & \text{if } \pi(A_j, k_j, M) < (1 + r_j)b_j \end{cases}$$

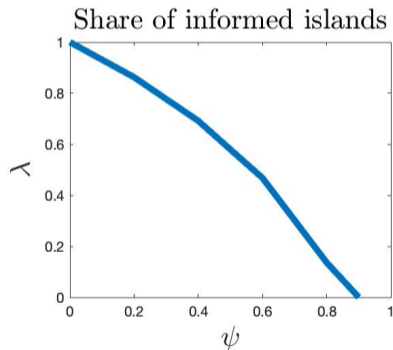
- ▶ Alternatively, ψ from bank's limited liability (deposit vs equity funding or govmt guarantees)

STAGE 1 - MORAL HAZARD AND INATTENTION

- Set c_{info} such that if $\psi = 0$, full information is optimal: $\lambda = 1$
 - ▶ $c \approx 3\%$ of average firm profits in full information

⇒ If limited liability $\uparrow \psi$, optimal information $\downarrow \lambda$

- **Intuition:** Lower exposure of manager to losses, lower incentive to collect information
(Mackowiak and Wiederholt, 2012, Lindbeck and Weibull, 2017)



CALIBRATION

Table: Calibration

Parameter	Interpretation	Value	Source
α	Firm profit function curvature	0.624	Implied by 20% markup and 1/3 cap share
ν	Return to scale final good sector	0.5	Implied by 50% markup and 1/2 interm share
r^f	Risk free rate	0.1	5-year return from quarterly 2%
ϕ	Investment adj cost coefficient	1	Literature (e.g. Gao et al, 2021)
σ_θ	Volatility aggregate shock	0.2	Unconditional volatility implied by $\rho = .995$ and $\sigma = 0.02$
σ_e	Volatility local shock	0.6	Three times aggregate volatility (inside literature interval)
σ_η	Volatility signal noise	0.64	Same as total TFP volatility
ψ	Compensation convexity	0	Normalization
c_d	Default cost	0.5	Baseline
τ	Corporate tax	0.20	(CBO, 2017)
c	Information cost	0.0017	Calibrated such that $\lambda = 1$ if $\psi = 0$

STAGE 2 - DISPERSED INFORMATION ($\lambda = 0$): RATIONAL EXTRAPOLATION

1. **Dotted black line:**
prior belief on revenues
2. **Dashed red line:**
posterior revenues of *informed* agents
(both **PE** and **GE** effect)

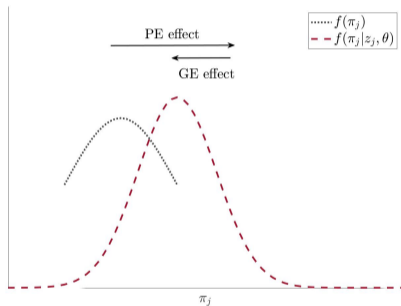


Figure: PE and GE effect after $\theta > 0$ shock

STAGE 2 - DISPERSED INFORMATION ($\lambda = 0$): RATIONAL EXTRAPOLATION

1. **Dotted black line:**
prior belief on revenues
2. **Dashed red line:**
posterior revenues of *informed* agents
(both **PE** and **GE** effect)
3. **Solid blue line:**
posterior revenues of *uninformed* agents
(only **PE** effect)

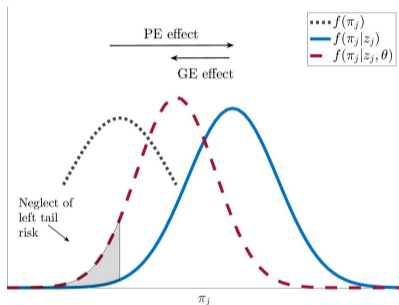


Figure: PE and GE effect after $\theta > 0$ shock